

**GENERAL TOPOLOGY  
HOMEWORK FOR WEEK 2**

DEADLINE: MON 11.3, 23:59

**Exercise 1.** *Let  $X$  be a Hausdorff space and suppose that  $(x_n), (y_n)$  are two sequences in  $X$  which converge to points  $x$  and  $y$  respectively. Furthermore, assume that for every  $n \in \mathbb{N}$  and every neighbourhood  $U$  of  $x_n$ , there is a  $m \geq n$  such that  $y_m \in U$ . Prove that  $x = y$ .*

**Exercise 2.** *Let  $f : X \rightarrow Y$  be a function between topological spaces which is **locally open**, meaning that for every point  $x \in X$  there exists a neighbourhood  $U_x$  of  $x$  such that  $f|_{U_x} : U_x \rightarrow Y$  is an open map. Prove that  $f$  is an open map.*