

**GENERAL TOPOLOGY  
HOMEWORK FOR WEEK 3**

DEADLINE: MON 18.3, 23:59

**Exercise 1.** *Prove this statement of Theorem 2.11: If the topology on  $X$  is induced by a family of maps  $f_i : X \rightarrow Y_i, i \in I$ , then a map  $g : Z \rightarrow X$  is continuous if and only if  $f_i \circ g : Z \rightarrow Y_i$  is continuous for all  $i \in I$ .*

**Exercise 2.** *Let  $(x_n) \subset X$  be a sequence converging to a point  $a \in X$ . Prove that the set  $A = \{a\} \cup \{x_n : n \in \mathbb{Z}_+\}$  is compact.*