

**GENERAL TOPOLOGY**  
**HOMEWORK FOR WEEK 4**

DEADLINE: MON 25.3, 23:59

**Exercise 1.** *Let  $A, B \subset X$  be open sets such that  $A \cup B$  and  $A \cap B$  are connected. Show that  $A$  and  $B$  are connected.*

Another formulation for  $X$  being a **normal space** is that for every two open sets  $U, V \subset X$  such that  $U \cup V = X$ , there exist closed sets  $A \subset U$  and  $B \subset V$  such that  $A \cup B = X$ .

(This is easy to prove with de Morgan's laws, you don't need to do it here but should check it for yourself.)

**Exercise 2.** *Let  $f : X \rightarrow Y$  be a continuous and closed surjection. Prove that if  $X$  is normal, then  $Y$  is normal.*